



This calculations policy has been developed in line with the National Curriculum (NC) for mathematics and the Calculation Guidance for Primary Schools developed by the National Centre of Excellence in Teaching Mathematics (NCETM).

The following statements from the NC have been central to the development of this policy:

- The principal focus of mathematics teaching in key stage 1 is to ensure that pupils develop confidence and mental fluency with whole numbers, counting and place value
- By the end of year 2, pupils should know the number bonds to 20 and be precise in using and understanding place value. An emphasis on practice at this early stage will aid fluency.

Similarly, we follow the NCETM advice that children should be “helped at an early stage to start calculating, rather than relying on ‘counting on’ as a way of calculating.” For this reason, we have focused on developing children’s ability to subitize in order to build up fluency with number bonds to 10 and then 20. These facts must be **MEMORISED** and thus, **it is essential that these skills are practised daily.**

In calculating, mathematical understanding is developed through use of representations that are first of all concrete (e.g. Dienes, apparatus), then pictorial (e.g. array, place value counters) to then facilitate abstract working (e.g. columnar addition, long multiplication).

According to the NCETM, “Informal methods of recording calculations are an important stage to help children develop fluency with formal methods of recording. A noticeable difference, however, that the LPS teachers observed in Shanghai is that these **were only used for a short period, to help children understand the internal logic of formal methods of recording calculations. They are stepping stones to formal written methods.** Here is an example from a Shanghai textbook:

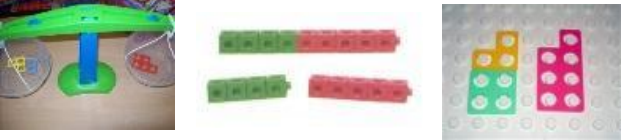
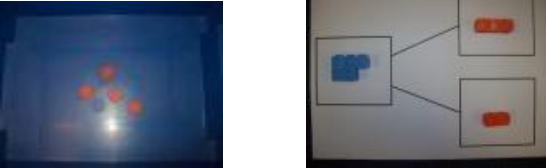
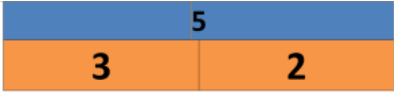
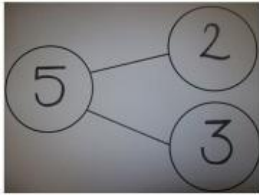


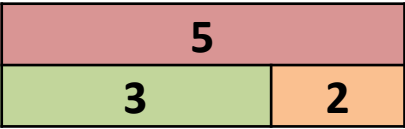
Thus, informal or ‘expanded methods’ are to be used only to illustrate/explain the formal method and should not be taught as an end in itself.

$$23 \times 4 = ?$$

$$\begin{array}{r} 23 \\ \times 4 \\ \hline 12 \\ 80 \\ \hline 92 \end{array}$$

$$\begin{array}{r} 23 \\ \times 4 \\ \hline 92 \end{array}$$


**ALWAYS SHOW THE CORRESPONDENCE BETWEEN CONCRETE/PICTORIAL METHOD and FORMAL WRITTEN METHOD**

Objective	Concrete	Pictorial	Abstract
To add numbers to 10	  <p>Children should be consistently shown <i>visually</i> that if <math>3+4=7</math> then <math>7-4=3</math> and <math>7-3=4</math></p>	 	$5 = 3 + 2$ $3 + 2 = 5$ $2 + 3 = 5$ $5 = 2 + 3$
Interpret mathematical statements	 <div data-bbox="801 842 1048 951" style="border: 1px solid black; padding: 5px; width: fit-content;">       Key focus is on understanding the meaning of =     </div> <div data-bbox="421 1230 600 1339" style="border: 1px solid black; padding: 5px; width: fit-content;">       What do I <b>add</b> to this side to make it balance? ?     </div>  <div data-bbox="869 1198 1066 1355" style="border: 1px solid black; padding: 5px; width: fit-content;">       What do I <b>subtract</b> from this side to make it balance?     </div>		$5 = 3 + 2$ $3 + 2 = 5$ $2 + 3 = 5$ $5 = 2 + 3$

To subtract numbers to 10


e.g.

$2 + 3 = 5$   
 (is the same as)

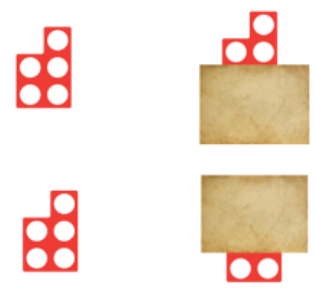
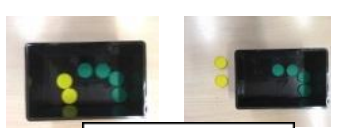


To show the corresponding subtraction facts

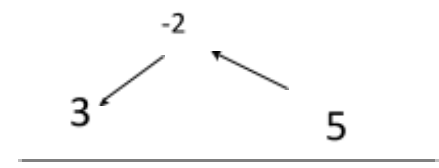
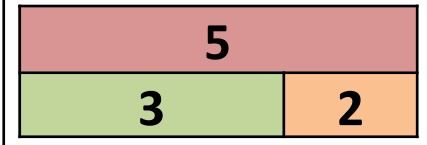
$5 - 2 = 3$   
 (is the same as)



We could achieve the same thing by covering part of the numicon: e.g.

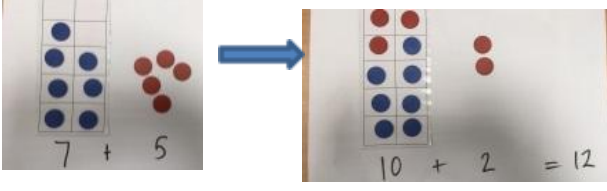


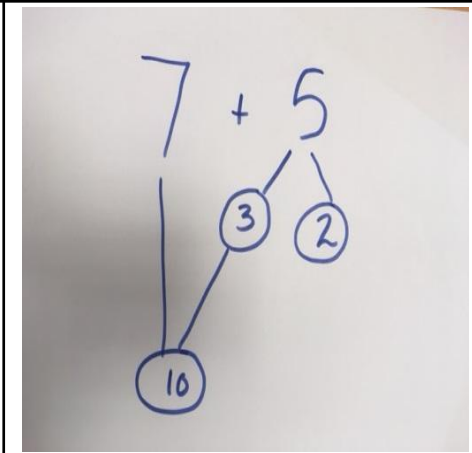



I have 6 in the box  
 and take 2 out –  
 what's left ? DON'T  
 LET THEM SEE !!



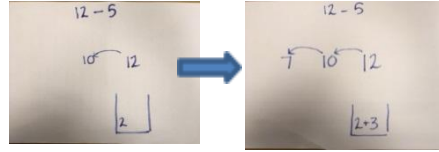
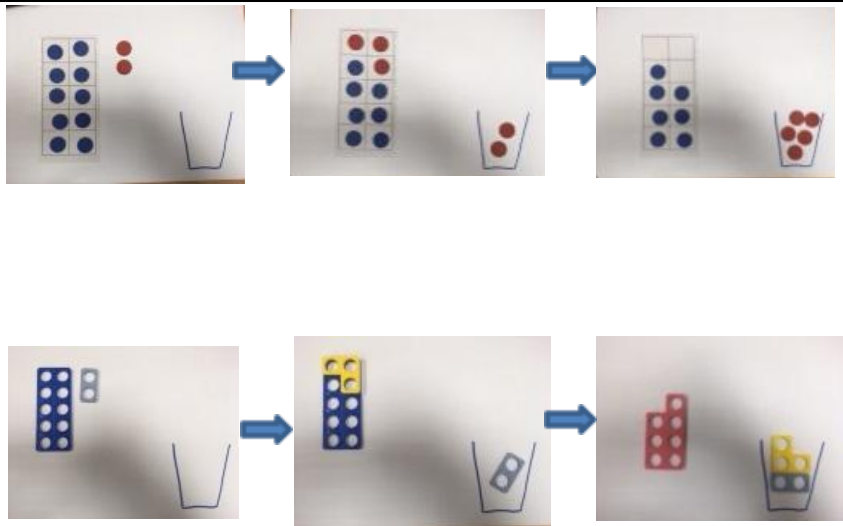
$5 - 2 = 3$   
 $3 = 5 - 2$

To add numbers across a tens boundary

$7 + 5 = 12$   
 $12 = 7 + 5$

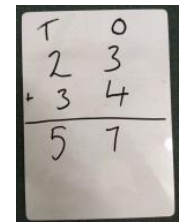
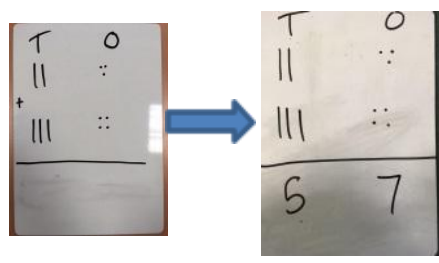
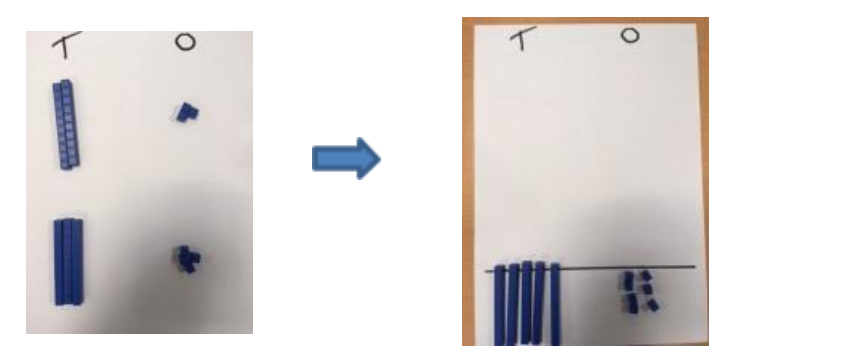
To subtract numbers across a tens boundary



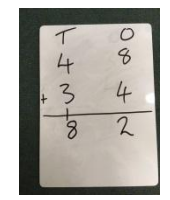
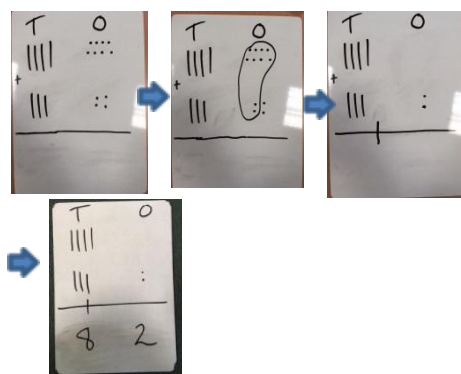
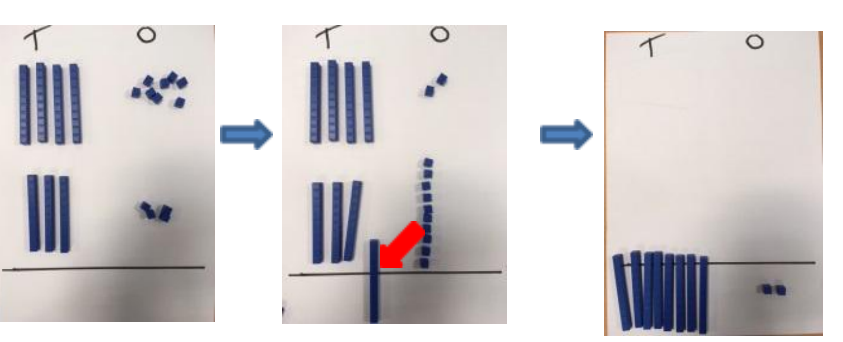
$$12 - 5 = 7$$

$$7 = 12 - 5$$

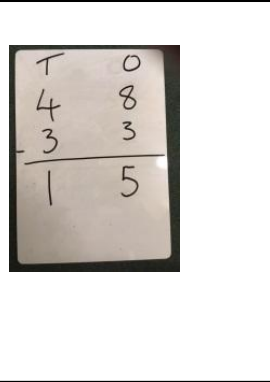
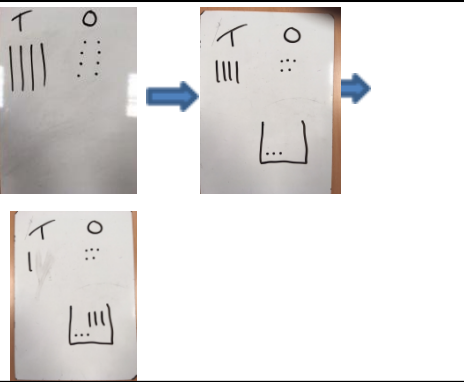
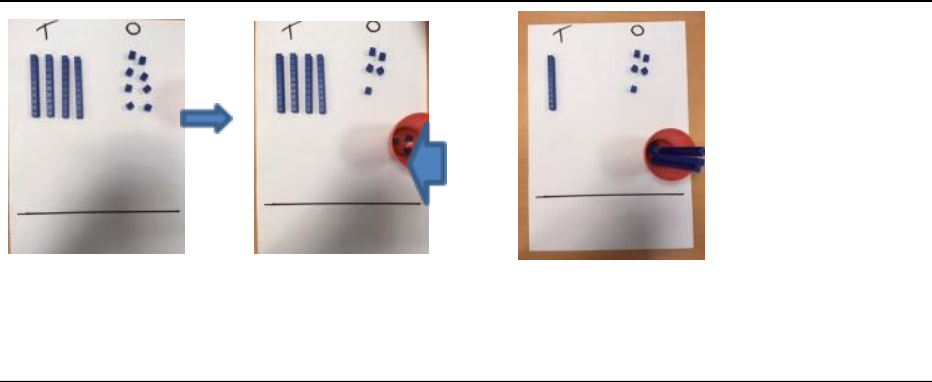
To add 2 digit numbers (no exchange)



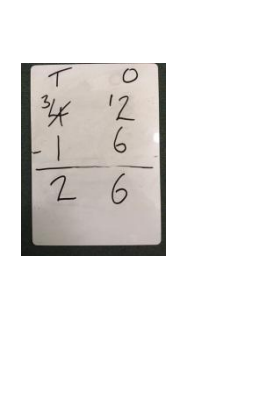
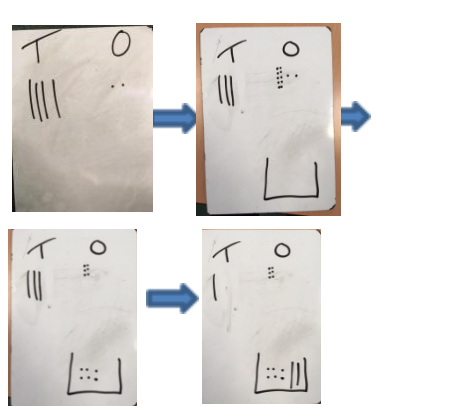
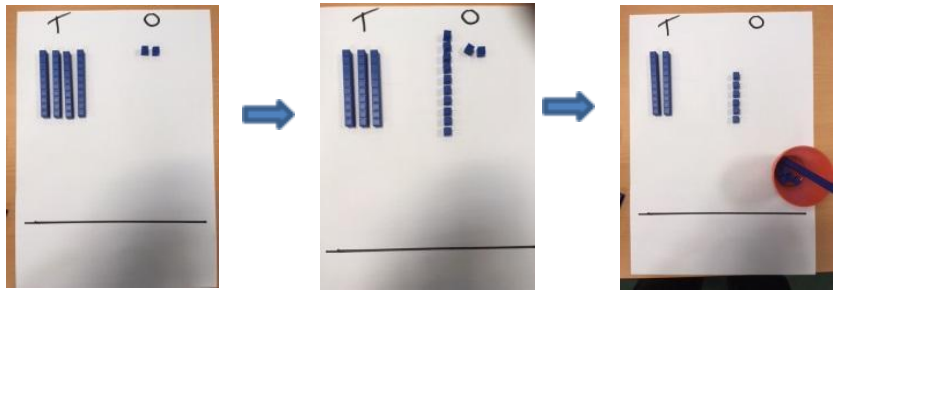
To add 2 digit numbers (with exchange)



To subtract 2 digit numbers (with no exchange)



To subtract 2 digit numbers (with exchange)



Double single digit numbers

Use practical activities using manipulatives including cubes and Numicon to demonstrate doubling

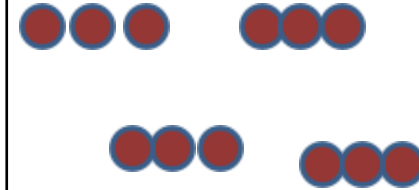
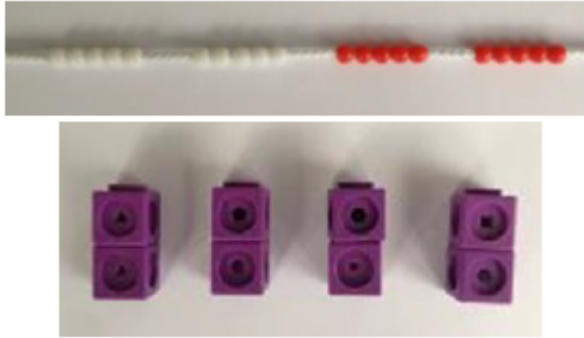
double 4 is 8  
 $4 \times 2 = 8$

Draw pictures to show how to double numbers

Double 4 is 8

$4 \times 2 = 8$

Counting in multiples




$$4 \times 3 = 12$$

$$3 \times 4 = 12$$

Making equal groups



Use manipulatives to create equal groups.

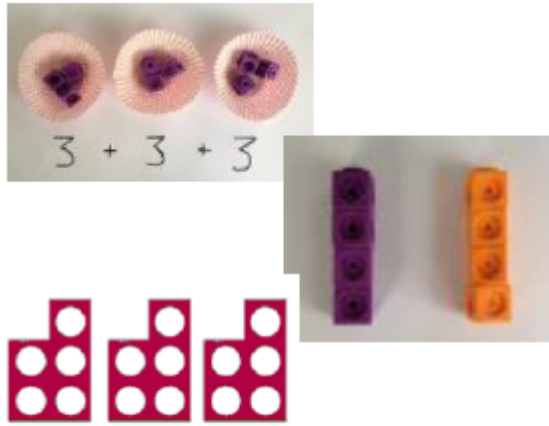
Draw  to show  $2 \times 3 = 6$

Draw and make representations

$$3 \times 2 = 6$$

$$2 \times 3 = 6$$

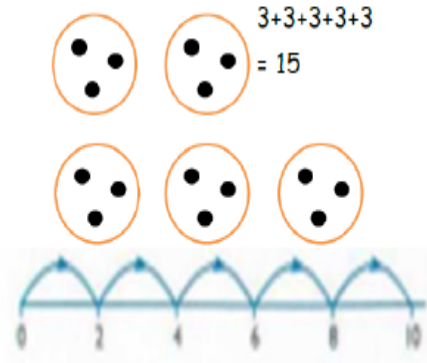
Multiplication as repeated addition



Use different objects to add equal groups

Use pictorial including number lines to solve

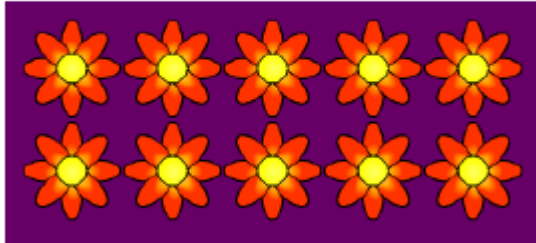
prob There are 3 sweets in one bag.  
How many sweets are in 5 bags altogether?



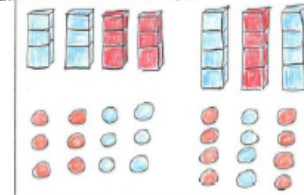
$$5 \times 3 = 15$$
$$3 \times 5 = 15$$

Using arrays

Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.



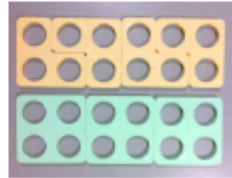
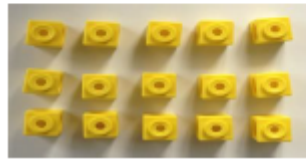
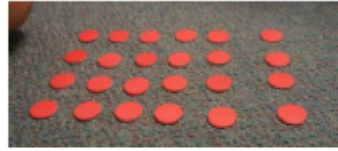
Draw representations of arrays to show understanding



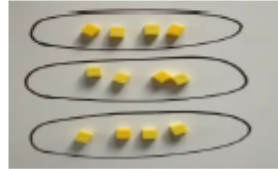
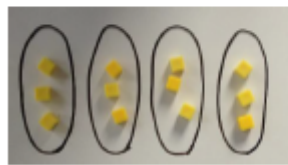
$$4 \times 3 = 12$$
$$3 \times 4 = 12$$

Multiplication is commutative

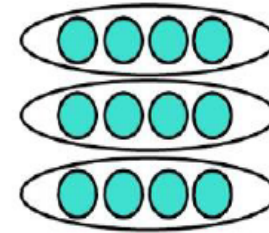
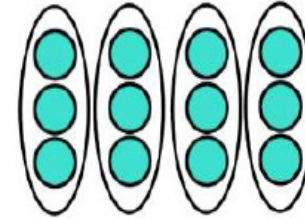
Create arrays using counters and cubes and Numicon.



Pupils should understand that an array can represent different equations and that, as multiplication is commutative, the order of the multiplication does not affect the answer.



Use representations of arrays to show different calculations and explore commutativity.



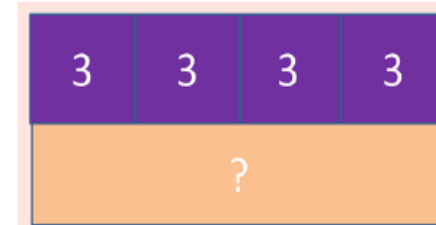
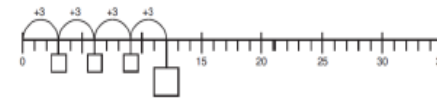
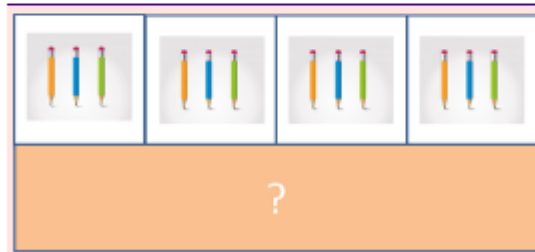
$$12 = 3 \times 4$$

$$12 = 4 \times 3$$

Counting in multiples



$$5 + 5 + 5 + 5 + 5 + 5 + 5 + 5 = 40$$

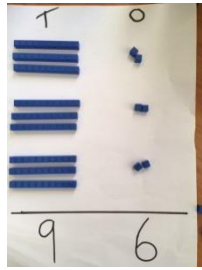




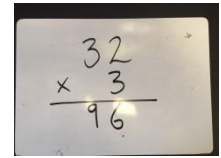
To multiply a two digit number by a one digit number (No exchange)

$$32 \times 3$$

Show as  
3 lots of  
32

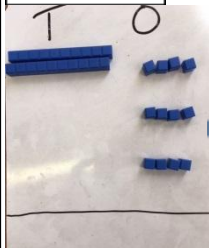


Secure the habit of multiplying the ones column **FIRST**

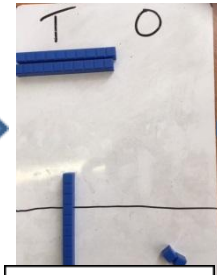


To multiply a two digit number by a one digit number (With exchange)

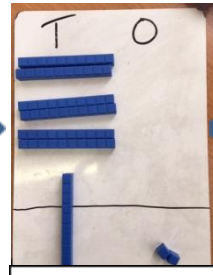
$$24 \times 3$$



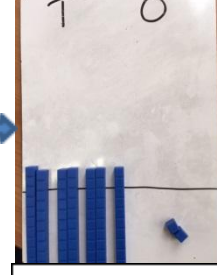
Ones column  
**FIRST**



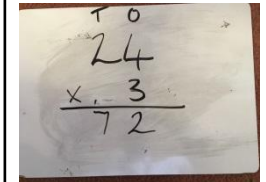
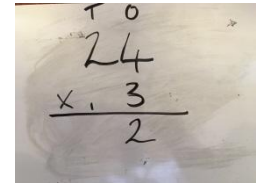
Exchange



Multiply tens

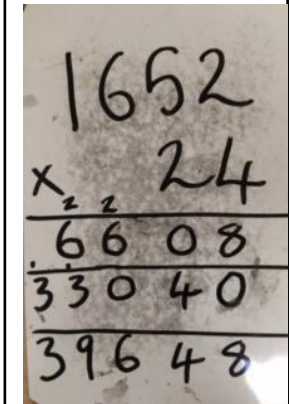
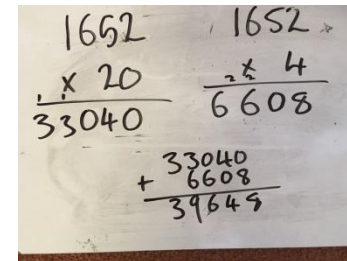


Total the 10s

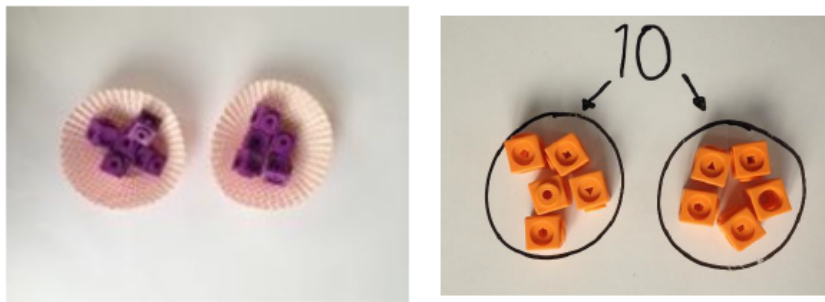


Multiply a 3 or 4 digit number by a 2 digit number

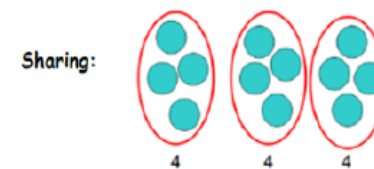
Preparatory step (see notes above)



Division as sharing



Children use pictures or shapes to share quantities.



12 shared between 3 is 4

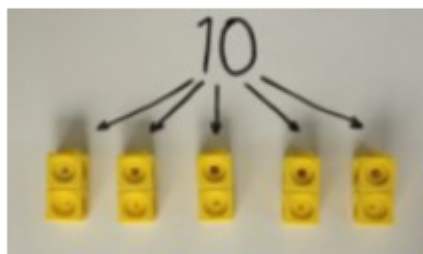
$$12 \div 3 = 4$$

$$12 \div 4 = 3$$

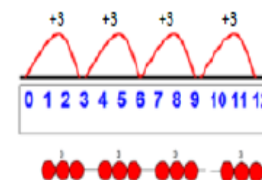
Division as grouping

Divide quantities into equal groups.

Use cubes, counters, objects or place value counters to aid understanding.



Use number lines for grouping



$$12 \div 3 = 4$$

Think of the bar as a whole. Split it into the number of groups you are dividing by and work out how many would be within each group.

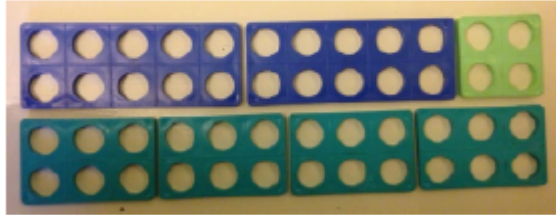


$$20 \div 5 = ?$$

$$5 \times ? = 20$$

Division as grouping  
(continued)

Use cubes, counters, objects or place value  
counters to aid understanding.

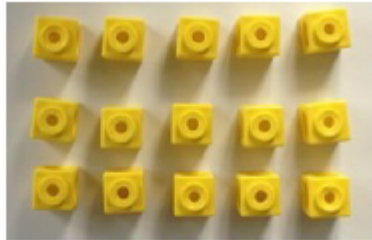


24 divided into groups of 6 = 4

$$96 \div 3 = 32$$



Division with arrays

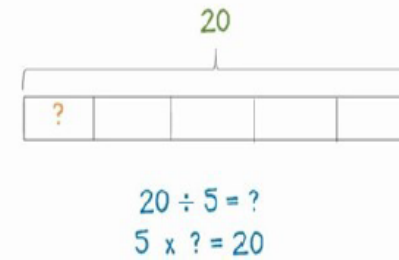


Link division to multiplication by creating an  
array and thinking about the number sentenc-  
es that can be created.

Eg  $15 \div 3 = 5$      $5 \times 3 = 15$

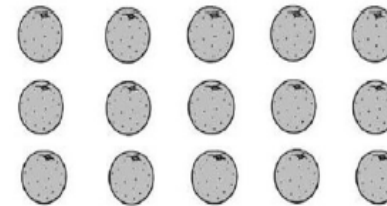
$15 \div 5 = 3$      $3 \times 5 = 15$

Continue to use bar modelling to aid solving  
division problems.



How many groups of 6 in  
24?  
 $24 \div 6 = 4$

Draw an array and use lines to split the array  
into groups to make multiplication and division  
sentences



Show links between  
division and  
multiplication facts

$$7 \times 4 = 28$$

$$4 \times 7 = 28$$

$$28 \div 7 = 4$$

$$28 \div 4 = 7$$

$$28 = 7 \times 4$$

$$28 = 4 \times 7$$

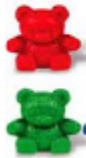
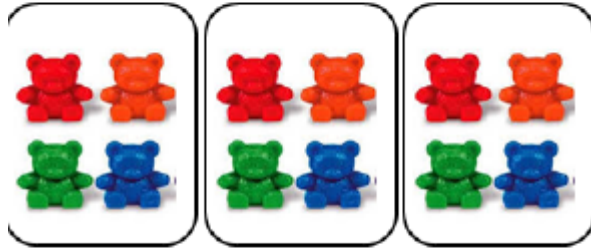
$$4 = 28 \div 7$$

$$7 = 28 \div 4$$

Division with remainders

$$14 \div 3 =$$

Divide objects between groups and see how much is left over



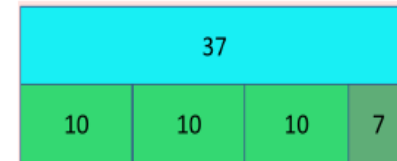
Jump forward in equal jumps on a number line then see how many more you need to jump to find a remainder.



Draw dots and group them to divide an amount and clearly show a remainder.



Use bar models to show division with remainders.



$$28 \div 5 = 5 \text{ r } 3$$

Short Division

$$\begin{array}{r} 218 \\ 4 \overline{) 872} \\ \underline{8} \phantom{00} \\ 7 \phantom{0} \\ \underline{7} \phantom{0} \\ 2 \phantom{0} \\ \underline{2} \\ 0 \end{array}$$
  

$$\begin{array}{r} 86 \text{ r } 2 \\ 5 \overline{) 432} \\ \underline{4} \phantom{00} \\ 3 \phantom{0} \\ \underline{3} \\ 2 \phantom{0} \\ \underline{2} \\ 0 \end{array}$$

Division by a single digit  
– extending to showing  
remainders as decimals

$$\begin{array}{r} 062.125 \\ 8 \overline{)4917.0000} \end{array}$$

Division by a two digit  
number  
(long and short method)

$$\begin{array}{r} 0364 \\ 21 \overline{)7644} \\ \underline{42} \phantom{00} \\ 63 \phantom{00} \\ \underline{84} \phantom{00} \\ 105 \phantom{00} \\ \underline{126} \phantom{00} \\ 147 \phantom{00} \\ \underline{168} \phantom{00} \\ 189 \phantom{00} \\ \underline{189} \\ 0 \end{array}$$

$$\begin{array}{r} 0364 \\ 21 \overline{)7644} \\ \underline{63} \phantom{00} \\ 126 \phantom{00} \\ \underline{84} \phantom{00} \\ 0 \end{array} \quad \begin{array}{r} 21 \\ 42 \\ 63 \\ 84 \\ 105 \\ 126 \\ 147 \\ 168 \\ 189 \\ 0 \end{array}$$

Encourage children  
to work out the  
timetable for the  
divisor